

CSCI-UA.0480-003 Parallel Computing

Lecture 9: MPI - III

Mohamed Zahran (aka Z) mzahran@cs.nyu.edu http://www.mzahran.com

Many slides of this lecture are adopted and slightly modified from:

- Gerassimos Barlas
- Peter S. Pacheco



int	MPI_Reduce(
	void *	input_data_p	/*	in	*/,
	void *	output_data_p	/*	out	*/,
	int	count	/*	in	*/,
	MPI_Datatype	datatype	/*	in	*/,
	MPI_Op	operator	/*	in	*/,
	int	dest_process	/*	in	*/,
	MPI_Comm	comm	/*	in	*/);

int MPI_Allreduce(

void *	input_data_p	/*	in	*/,
void *	output_data_p	/*	out	*/,
int	count	/*	in	*/,
MPI_Datatype	datatype	/*	in	*/,
MPI_Op	operator	/*	in	*/,
MPI_Comm	comm	/*	in	*/);

int MPI_Bcast(

void *	data_p	/*	in/out	*/,
int	count	/*	in	*/,
MPI_Datatype	datatype	/*	in	*/,
int	source_proc	/*	in	*/,
MPI_Comm	comm	/*	in	*/);

Collective

point-to-point

int MPI_Send(int	MPI_Recv(
						void *	msg_buf_p	/*	out	*/,
void *	msg_buf_p	/*	in	*/,		int	buf_size	/*	in	*/,
int	msg_size	/*	in	*/,		MPI_Datatype	buf_type	/*	in	*/,
MPI_Datatype	msg_type	/*	in	*/,		int	source	/*	in	*/.
int	dest	/*	in	*/,		int	taσ	/*	in	*/.
int	tag	/*	in	*/,		WDT G		,		,
MPT Comm	communicator	/*	in	*/):		MPI_COMM	communicator	/*	ın	*/,
				,		MPI_Status*	status_p	/*	out	*/);

Data distributions

$$\mathbf{x} + \mathbf{y} = (x_0, x_1, \dots, x_{n-1}) + (y_0, y_1, \dots, y_{n-1})$$

= $(x_0 + y_0, x_1 + y_1, \dots, x_{n-1} + y_{n-1})$
= $(z_0, z_1, \dots, z_{n-1})$
= \mathbf{z}

void Vector_sum(double x[], double y[], double z[], int n) {
 int i;

```
for (i = 0; i < n; i++)
    z[i] = x[i] + y[i];
/* Vector_sum */</pre>
```

Sequential version

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}

Different partitions of a 12component vector among 3 processes



- **Block**: Assign blocks of consecutive components to each process.
- **Cyclic**: Assign components in a round robin fashion.
- Block-cyclic: Use a cyclic distribution of blocks of components.

Parallel implementation of vector addition

```
void Parallel_vector_sum(
    double local_x[] /* in */,
    double local_y[] /* in */,
    double local_z[] /* out */,
    int local_n /* in */) {
    int local_i;
    for (local_i = 0; local_i < local_n; local_i++)
        local_z[local_i] = local_x[local_i] + local_y[local_i];
} /* Parallel_vector_sum */</pre>
```

How will you distribute parts of x[] and y[] to processes?

Scatter

- Read an entire vector on process 0
- MPI_Scatter sends the needed components to each of the other processes.

<pre>int MPI_Scatter(</pre>					
void *	send_buf_p	/*	in	*/,	# data items going
int	send_count	<!--*</del-->	in	*/,	—— to each process
MPI_Datatype	send_type	/*	in	*/,	
void *	recv_buf_p	/*	out	*/,	
int	recv_count	/*	in	*/,	
MPI_Datatype	recv_type	/*	in	*/,	
int	src_proc	/*	in	*/,	
MPI_Comm	comm	/*	in	*/);	

Important:

- All arguments are important for the source process (process 0 in our example)
- For all other processes, only recv_buf_p, recv_count, recv_type, src_proc, and comm are important

Reading and distributing a vector

```
void Read vector(
     double
             local_a[] /* out */,
              local n /* in */,
     int
                      /* in */.
     int
               n
     char vec_name[] /* in */,
                                                        process 0 itself
     int my rank /* in */.
     MPI_Comm comm /* in */) {
                                                      also receives data.
  double * a = NULL;
  int i:
  if (my rank == 0) {
     a = malloc(n*sizeof(double));
     printf("Enter the vector %s\n", vec_name);
     for (i = 0; i < n; i++)
        scanf("%lf", &a[i]);
     MPI Scatter(a, local n, MPI DOUBLE, local a, local n, MPI DOUBLE,
           0, \text{ comm});
     free(a);
  } else {
     MPI_Scatter(a, local_n, MPI_DOUBLE, local_a, local_n, MPI_DOUBLE,
           0. comm):
  /* Read_vector */
```

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int	MPI_Scatter(
	void *	send_buf_p	/*	in	*/,
	int	send_count	/*	in	*/,
	MPI_Datatype	send_type	/*	in	*/,
	void *	recv_buf_p	/*	out	*/,
	int	recv_count	/*	in	*/,
	MPI_Datatype	recv_type	/*	in	*/,
	int	src_proc	/*	in	*/,
	MPI Comm	comm	/*	in	*/);

send_buf_p

- is not used except by the sender.
- However, it must be defined or NULL on others to make the code correct.
- Must have at least communicator size * send_count elements
- All processes must call MPI_Scatter, not only the sender.
- send_count the number of data items sent to each process.
- recv_buf_p must have at least send_count elements
- MPI_Scatter uses block distribution



Gather

• MPI_Gather collects all of the components of the vector onto process dest process, ordered in rank order.

int	MPI_Gather(
	void *	send_buf_p	/*	in	*/,
	int	send_count	/*	in	*/,
	MPI_Datatype	send_type	/*	in	*/,
	void *	recv_buf_p	/*	out	*/,
	int	recv_count	/*	in	*/,
	MPI_Datatype	recv_type	/*	in	*/,
	int	dest_proc	/*	in	*/,
	MPI Comm	comm	/*	in	*/);

Important:

- All arguments are important for the destination process.
- For all other processes, only send_buf_p, send_count, send_type, dest_proc, and comm are important

Print a distributed vector (1)

void Print_vector(

double	local_b[]	/*	in	*/,
int	local_n	/*	i n	*/,
int	n	/*	in	*/,
char	title[]	/*	i n	*/,
int	my_rank	/*	i n	*/,
MPI_Comm	comm	/*	in	*/) {

double * b = NULL; int i;

Print a distributed vector (2)

```
if (my_rank == 0) {
   b = malloc(n*sizeof(double));
   MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE,
         0. \text{ comm}):
   printf("%s\n", title);
   for (i = 0; i < n; i++)
      printf("%f ", b[i]);
   printf("\n");
   free(b);
} else {
   MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE,
         0, \text{ comm});
/* Print_vector */
```

- Allgather
 Concatenates the contents of each process' send_buf_p and stores this in each process' recv_buf_p.
- As usual, recv_count is the amount of data being received from each process.

```
int MPI_Allgather(
     void *
                 send_buf_p /* in */,
                 send_count /* in */,
     int
                 send_type /* in */,
     MPI_Datatype
     void *
                 recv_buf_p /* out */,
                 recv_count /* in */,
     int
                 recv_type /* in */,
     MPI Datatype
     MPI Comm
                 comm /* in */):
```



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Matrix-vector multiplication

<i>a</i> ₀₀	<i>a</i> 01	•••	$a_{0,n-1}$		УО
<i>a</i> ₁₀	<i>a</i> ₁₁	•••	$a_{1,n-1}$	<i>x</i> 0	У1
:	:		:	<i>x</i> ₁	:
a_{i0}	a_{i1}	•••	$a_{i,n-1}$: =	$y_i = a_{i0}x_0 + a_{i1}x_1 + \dots + a_{i,n-1}x_{n-1}$
<i>a_{i0}</i>	<i>a_{i1}</i>		$a_{i,n-1}$:	\vdots	$y_i = a_{i0}x_0 + a_{i1}x_1 + \cdots + a_{i,n-1}x_{n-1}$:

Pseudo-code Serial Version



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Serial matrix-vector multiplication

void Mat_vect_mult(double A[] /* in */,**double** x[] /* *in* */, **double** y[] /* out */, int m /* in */, int n /* in */) { int i, j; for (i = 0; i < m; i++) { y[i] = 0.0;for (j = 0; j < n; j++)y[i] += A[i*n+j]*x[j];/* Mat_vect_mult */

Let's assume x[] is distributed among the different processes

An MPI matrix-vector multiplication function (1)

void Mat_vect_mu	ilt(
double	local_A[]	/*	in	*/,
double	local_x[]	/*	in	*/,
double	local_y[]	/*	out	*/,
int	local_m	/*	in	*/,
int	n	/*	in	*/,
int	local_n	/*	in	*/,
MPI_Comm	comm	/*	in	*/) {
double * x;				
<pre>int local_i,</pre>	j;			
int local_ok	= 1;			

An MPI matrix-vector multiplication function (2)

```
for (local_i = 0; local_i < local_m; local_i++) {
    local_y[local_i] = 0.0;
    for (j = 0; j < n; j++)
        local_y[local_i] += local_A[local_i*n+j]*x[j];
}
free(x);
/* Mat_vect_mult */</pre>
```

Keep in mind ...

- In distributed memory systems, communication is more expensive than computation.
- Distributing a fixed amount of data among several messages is more expensive than sending a single big message.

Derived datatypes

- Used to represent any collection of data items
- If a function that sends data knows this information about a collection of data items, it can collect the items from memory before they are sent.
- A function that receives data can distribute the items into their correct destinations in memory when they're received.

Derived datatypes A sequence of basic MPI data types together with a displacement for each of the data types.



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MPI_Type create_struct

 Builds a derived datatype that consists of individual elements that have different basic types.



an integer type that is big enough to store an address on the system.

From the address of item 0

int MPI_Get_address(
 void * location_p /* in */,
 MPI_Aint* address_p /* out */);

Before you start using your new data type

int MPI_Type_commit(MPI_Datatype* new_mpi_t_p /* in/out */);

Allows the MPI implementation to optimize its internal representation of the datatype for use in communication functions.

When you are finished with your new type

int MPI_Type_free(MPI_Datatype* old_mpi_t_p /* in/out */);

This frees any additional storage used.

Example (1)

void	<pre>Build_mpi_type(</pre>					
	double *	a_p	/*	in	*/,	
	double *	b_p	/*	in	*/,	
	int *	n_p	/*	in	*/,	
	MPI_Datatype*	input_mpi_t_p	/*	out	*/) {	

```
int array_of_blocklengths[3] = {1, 1, 1};
MPI_Datatype array_of_types[3] = {MPI_DOUBLE, MPI_DOUBLE, MPI_INT};
MPI_Aint a_addr, b_addr, n_addr;
MPI_Aint array_of_displacements[3] = {0};
```

Example (2)

```
MPI_Get_address(a_p, &a_addr);
MPI_Get_address(b_p, &b_addr);
MPI_Get_address(n_p, &n_addr);
array_of_displacements[1] = b_addr-a_addr;
array_of_displacements[2] = n_addr-a_addr;
MPI_Type_create_struct(3, array_of_blocklengths,
array_of_displacements, array_of_types,
input_mpi_t_p);
MPI_Type_commit(input_mpi_t_p);
} /* Build_mpi_type */
```

Example (3)

Build_mpi_type(a_p, b_p, n_p, &input_mpi_t);

```
if (my_rank == 0) {
    printf("Enter a, b, and n\n");
    scanf("%lf %lf %d", a_p, b_p, n_p);
}
MPI_Bcast(a_p, 1, input_mpi_t, 0, MPI_COMM_WORLD);
MPI_Type_free(&input_mpi_t);
```

The receiving end can use the received complex data item as if it is a structure.

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/* Get_input */



MEASURING TIME IN MPI

We have seen in the past ...

- time in Linux
- clock() inside your code
- Does MPI offer anything else?

Elapsed parallel time

 Returns the number of seconds that have elapsed since some time in the past.

How to Sync Processes?

MPI_Barrier

 Ensures that no process will return from calling it until every process in the communicator has started calling it.

int MPI_Barrier(MPI_Comm comm /* in */);



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Let's see how we can analyze the performance of and MPI program The matrix-vector multiplication



if (my_rank == 0)
 printf("Elapsed time = %e seconds\n", elapsed);

Run-times of serial and parallel matrix-vector multiplication

		Order of Matrix									
comm_sz	1024	2048	4096	8192	16,384						
1	4.1	16.0	64.0	270	1100						
2	2.3	8.5	33.0	140	560						
4	2.0	5.1	18.0	70	280						
8	1.7	3.3	9.8	36	140						
16	1.7	2.6	5.9	19	71						

(Seconds)

Speedups of Parallel Matrix-Vector Multiplication

	Order of Matrix						
comm_sz	1024	2048	4096	8192	16,384		
1	1.0	1.0	1.0	1.0	1.0		
2	1.8	1.9	1.9	1.9	2.0		
4	2.1	3.1	3.6	3.9	3.9		
8	2.4	4.8	6.5	7.5	7.9		
16	2.4	6.2	10.8	14.2	15.5		

Efficiencies of Parallel Matrix-Vector Multiplication

	Order of Matrix						
comm_sz	1024	2048	4096	8192	16,384		
1	1.00	1.00	1.00	1.00	1.00		
2	0.89	0.94	0.97	0.96	0.98		
4	0.51	0.78	0.89	0.96	0.98		
8	0.30	0.61	0.82	0.94	0.98		
16	0.15	0.39	0.68	0.89	0.97		

Conclusions

- Reducing messages is a good performance strategy!
 – Collective vs point-to-point
- Distributing a fixed amount of data among several messages is more expensive than sending a single big message.